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| COMPUTER APPLICATIONS IN IME - MEE212 | Quiz 1 - Matlab 119 MINUTES |  |
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| PROBLEM 1 (25 PTS) | PROBLEM 2 (50 PTS) | PROBLEM 3 (25 PTS) | TOTAL (100 PTS) |
| :--- | :---: | :---: | :---: |

## READ BEFORE YOU START:

- No questions are allowed.
- Write your name and ID before you start. You are not allowed to take the exam handout with you.
- The quiz handouts will be collected on 12:55 PM.
- Before you start create a folder on the Desktop using you FIRST_LAST name.
- SAVE ALL YOUR FILES IN THAT FOLDER BEFORE 12:59 PM.
- It is your responsibility to save your work before the test ends. No files will be collected afterwards what so ever.
- Attempt all problems to get partial grades.
- UNLESS SPECIFIED, values should NOT be displayed in MATLAB's command window.
- Log in to the workstations using the following credentials (Case sensitive): User= mee.exam | Pass= GLuckHf


## Problem 1 - matrix manipulation ( 25 points)

Perform the following matrix manipulations in a single script file (add \%comments to separate problem parts).
a. Create the two matrices $\boldsymbol{A}$ and $\boldsymbol{B}$

$$
A=\left[\begin{array}{cc}
25 & 58 \\
13 & 31 \\
5 & 62 \\
6 & 2 \\
8 & 12
\end{array}\right] \quad B=\left[\begin{array}{ccccc}
1 & 4 & 5 & 3 & 2 \\
5 & 7 & 2 & 9 & 6 \\
8 & 10 & 15 & 22 & 6
\end{array}\right]
$$

b. Concatenate $\boldsymbol{A}$ and $\boldsymbol{B}$ into one $5 \times 5$ matrix $\boldsymbol{C}$ by taking the transpose of $\boldsymbol{B}$ and inserting it to the right of $\boldsymbol{A}$.

$$
\text { i.e. } C=\left[\begin{array}{ccccc}
25 & 58 & 1 & 5 & 8 \\
13 & 31 & 4 & 7 & 10 \\
5 & 62 & 5 & 2 & 15 \\
6 & 2 & 3 & 9 & 22 \\
8 & 12 & 2 & 6 & 6
\end{array}\right]
$$

c. Calculate the determinant of $\boldsymbol{C}$ and save it in a variable called $\boldsymbol{C}_{-}$det. Disply $\boldsymbol{C}_{-}$det in the workspace.
d. Find the inverse of $\boldsymbol{C}$ and save it in a variable called $\boldsymbol{D}$.
e. Extract the $\boldsymbol{C}$ the elements highlighted below and save it in a variable called $\boldsymbol{E}$.

$$
C=\left[\begin{array}{ccccc}
25 & 58 & 1 & 5 & 8 \\
13 & 31 & 4 & 7 & 10 \\
5 & 62 & 5 & 2 & 15 \\
6 & 2 & 3 & 9 & 22 \\
8 & 12 & 2 & 6 & 6
\end{array}\right]
$$

## Problem 2 - functions and applications ( 50 points)

It is required to find the radial deflection across the wall of a pressure vessel subject to internal pressure. For a thick pressure vessel of inner radius $\boldsymbol{a}$ and outer radius $\boldsymbol{b}$, the differential equation for the radial deflection of a point along the thickness is given by:

$$
\frac{d^{2} u}{d r^{2}}+\frac{1}{r} \frac{d u}{d r}-\frac{u}{r^{2}}=0
$$

The deflection $\boldsymbol{u}$ (in inch) at the boundaries is related to the pressure $\boldsymbol{P}$ (in psi) inside the vessel by:

$$
\begin{aligned}
& \left.u\right|_{r=a}=5.2 \times 10^{-5} P-1.45 \times 10^{-7} \\
& \left.u\right|_{r=b}=-3 \times 10^{-11} P^{2}+2.1 \times 10^{-5} P-14.5 \times 10^{-5}
\end{aligned}
$$

Given the symmetry of the pressure vessel, the problem can be simplified into a 1 D domain as shown in the figure


You are required to use the finite difference method to discretize the 1D domain and find the deflection distribution across the wall of a vessel that has an inside diameter of 10 " and a wall thickness of 1.5 " by doing the following:
a. Create a function called "PressureVessel" that will find the deflection across the wall thickness. The function inputs should be: $\boldsymbol{N}$ (the number of discretization elements) and $\boldsymbol{P}$ (the pressure inside the vessel). The function should return 2 arrays: the radial coordinates of the nodes $r$ and the deflection magnitude at these coordinates $\boldsymbol{d}$ (Both should be $\mathbf{N + 1}$ in size).

The finite difference approximations of the differential equation terms are given by:

$$
\begin{gathered}
\frac{d^{2} u}{d r^{2}} \approx \frac{u_{i+1}-2 u_{i}+u_{i-1}}{(\Delta r)^{2}} \\
\frac{d u}{d r} \approx \frac{u_{i+1}-u_{i}}{\Delta r}
\end{gathered}
$$

b. Create a MATLAB script that will first prompt the user to input the number of discretization points ( $N$ ) and then use the "PressureVessel" function to solve the deflection distribution problem for the following pressure values: [ $P=25 \mathrm{psi}],[P=50 \mathrm{psi}],[P=100 \mathrm{psi}]$, and $[P=200 \mathrm{psi}]$ (Enter a value of 10 for $\boldsymbol{N}$ ). The script file should plot the deflection distribution of the 4 cases on a single figure with:

- Each curve should have a different color and a different marker.
- A legend showing the pressure of each curve (e.g. ' $P=25 p s i$ ', ' $P=50 p s i$ ', ...)
- The title of the figure should be: "Problem 2 Solution"
- The $x$-label of the figure should be: "Radial distance, inch"
- The y-label of the figure should be: "Deflection, inch"

NOTE: the figure coloring and labeling should be done programmatically (i.e. in the script file not manually with the figure editor).

## Problem 3 - plotting ( 25 points)

Solve this problem using a single script file (add \%comments to separate problem parts).
You should first generate the data that you are going to use in your plots using the following command:
L=membrane;
This will generate a $31 \times 31$ array that will be used in all the plots.
On a single figure containing $2 \times 2$ plots generate the following programatically:
a. Plot the data using the mesh plot; the $x$-axis label should be " $x$ ", the $y$-axis label should be " $y$ ", the $z$-axis label should be "Height", and the plot title should be "3D Mesh plot". Grid should be off. Plot should be on the upper left side of the figure.
b. Plot the data using the surf plot; the $x$-axis label should be " $x$ ", the $y$-axis label should be " $y$ ", the $z$-axis label should be "Height", and the plot title should be "3D Surface plot". Grid should be off. Shading should be interp (refer to MATLAB help on how to use the shading function). Plot should be on the upper right side of the figure.
c. Plot the data using the contour3 plot with 30 lines; the $x$-axis label should be " $x$ ", the $y$-axis label should be " $y$ ", the $z$-axis label should be "Height", and the plot title should be " 3 D Contour plot". Grid should be off. Plot should be on the lower left side of the figure.
d. Plot the data using the contourf plot with 10 lines; $x$-axis label should be " $x$ ", the $y$-axis label should be " $y$, and the plot title should be " $2 D$ Contour plot". Grid should be off. Plot should be on the lower right side of the figure.

The axis limits for the 3D plots should be $[030]$ for the $x$-axis, $[030]$ for the $y$-axis, and [ $\min (\mathrm{L}) \max (\mathrm{L})]$ for the $z$-axis.

